



CHISA 2018 PRAGUE

PRES 2018



## A CFD approach to study catalytic reactors filled with open cell foams

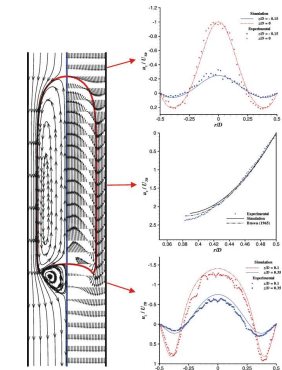
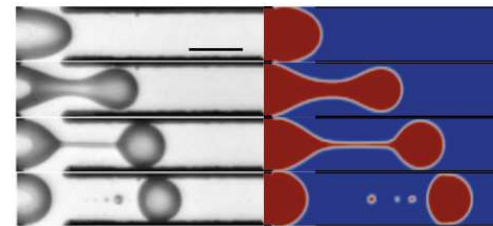
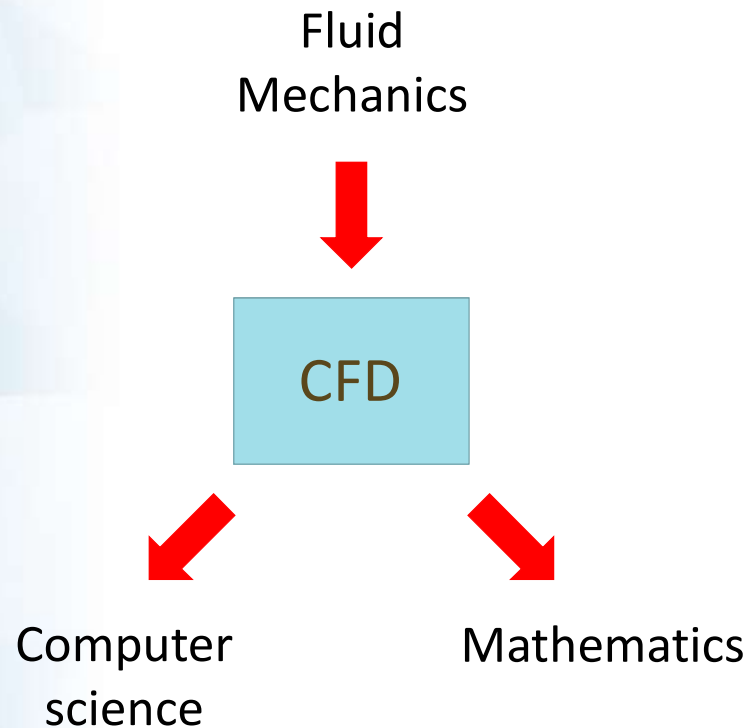
José Daniel Araújo, Daniel Direito and Manuel Alves



H2020: PRINTCR3DIT - Process Intensification through Adaptable Catalytic Reactors made by 3D Printing

[www.printcr3dit.eu](http://www.printcr3dit.eu)

## Computational Fluid Dynamics



### Main uses

- **Fundamental science: discover new phenomena**
- **Design and optimization: design and improve equipment**
- **Substitute for experiments and monitoring: modeling of existing equipment or natural phenomena**

## CFD simulations

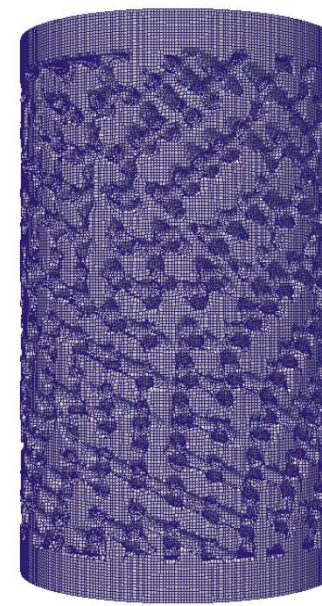
Foam structure  
(solid part)



Domain  
(fluid part)



Computational  
mesh



Software: OpenFOAM

## CFD simulations – tracer tests

### Fluid

Water properties

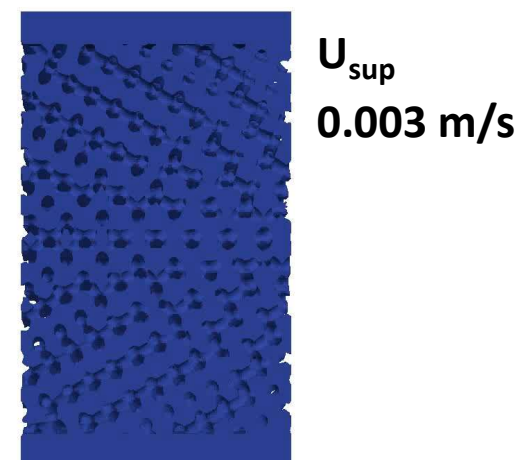
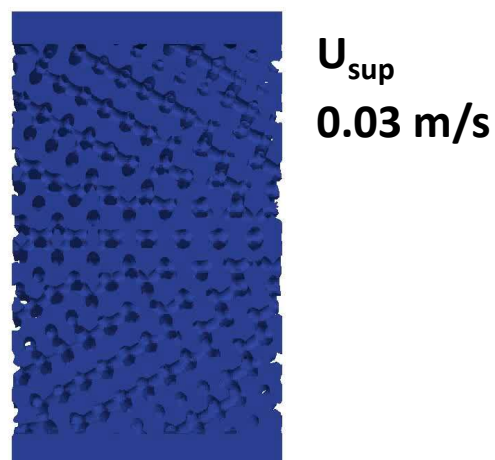
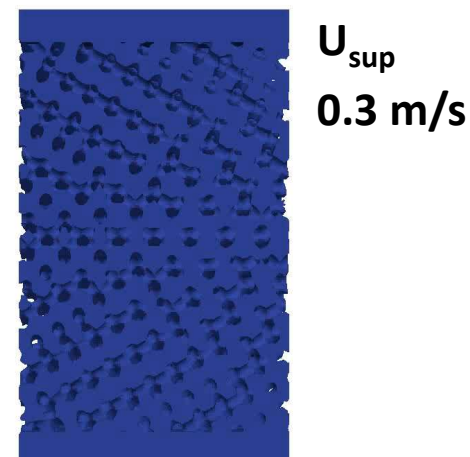
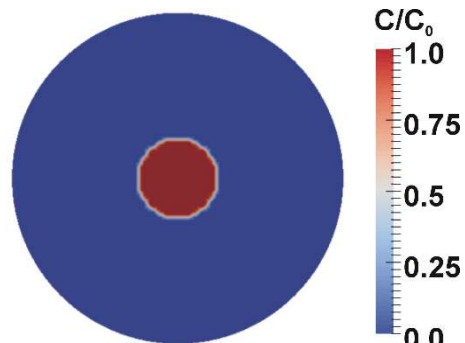
$$D_m = 1 \times 10^{-9} \text{ m}^2/\text{s}$$

### Domain

$$D = 2.08 \text{ cm}$$

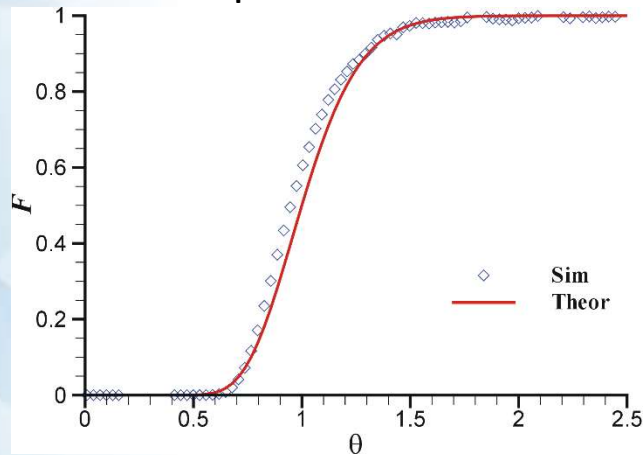
$$L = 3.50 \text{ cm}$$

$$\varepsilon = 0.56$$



## CFD simulations – tracer tests

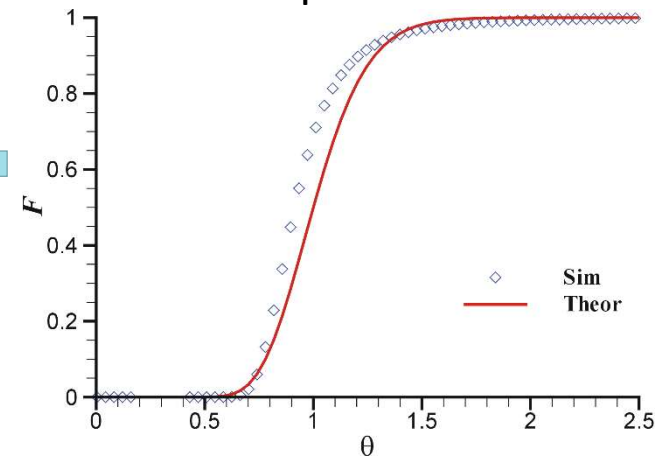
$U_{sup} = 0.3 \text{ m/s}$



$D_L \text{ (m}^2\text{/s)}$   
 $3.04 \times 10^{-5}$



$U_{sup} = 0.03 \text{ m/s}$

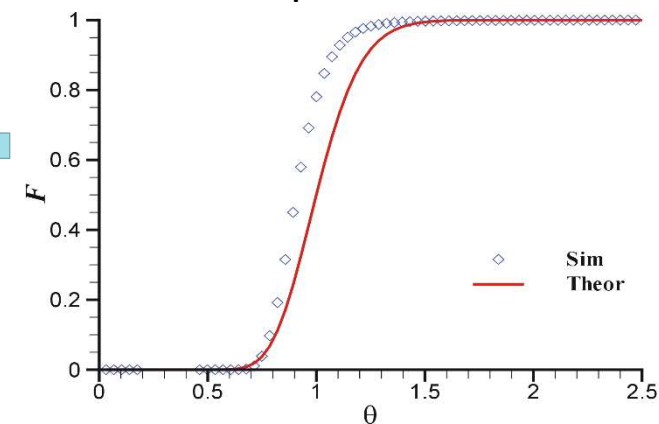


$D_L \text{ (m}^2\text{/s)}$   
 $3.50 \times 10^{-4}$

$D_L \text{ (m}^2\text{/s)}$   
 $2.11 \times 10^{-6}$



$U_{sup} = 0.003 \text{ m/s}$

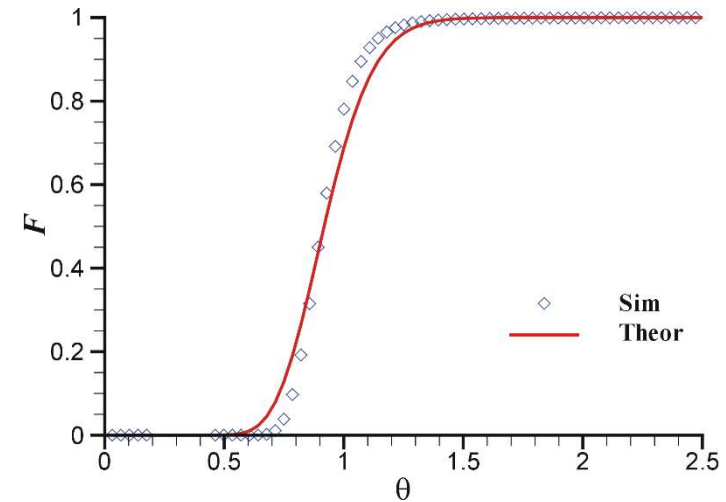
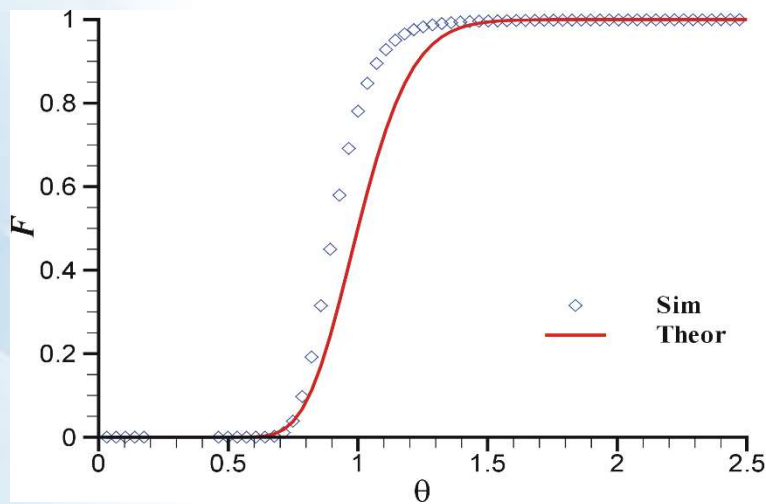


**Danckwerts (1953)**

$$F = \frac{C_{out}}{C_{in}} = \frac{1}{2} \left[ 1 - \operatorname{erf} \left( \frac{L - U_{sup} \cdot t}{2 \cdot \varepsilon \cdot \sqrt{D_L \cdot t}} \right) \right]$$

## CFD simulations – tracer tests

$U_{sup} = 0.003 \text{ m/s}$



$U_{sup} \text{ (m/s)}$   
**0.3**

- $D_L \text{ (m}^2\text{/s)}$   
 $3.50 \times 10^{-4}$
- $V_{dead} \text{ (%)}$   
**3.4**

$U_{sup} \text{ (m/s)}$   
**0.03**

- $D_L \text{ (m}^2\text{/s)}$   
 $3.04 \times 10^{-5}$
- $V_{dead} \text{ (%)}$   
**6.2**

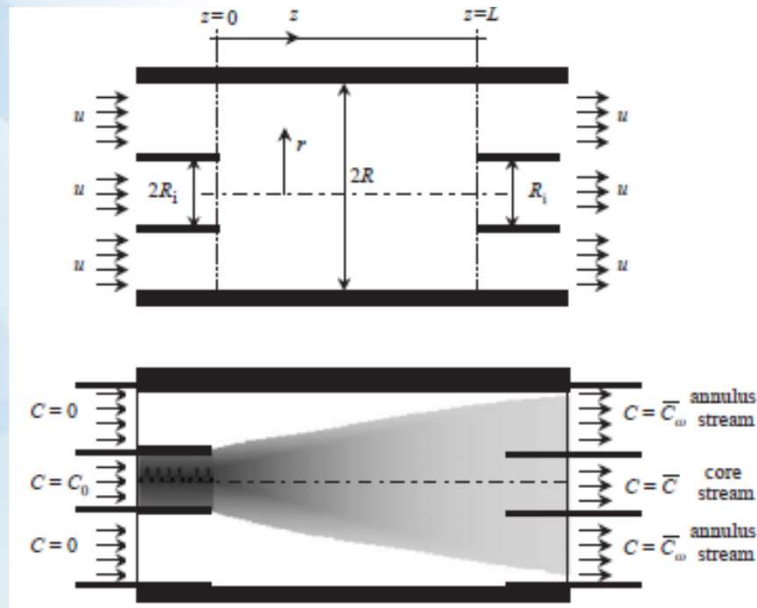
$U_{sup} \text{ (m/s)}$   
**0.003**

- $D_L \text{ (m}^2\text{/s)}$   
 $2.11 \times 10^{-6}$
- $V_{dead} \text{ (%)}$   
**8.2**

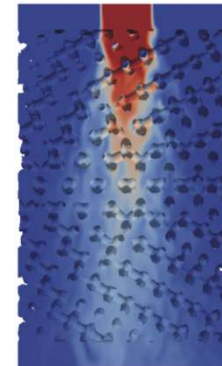
## CFD simulations – tracer tests

Hiby and Schummer (1960)

$$\frac{C_{out,core}}{C_{in,core}} = 4 \sum_0^{\infty} \frac{J_1^2(\lambda_n R_i/R)}{\lambda_n^2 J_0^2(\lambda_n)} \cdot \exp\left[-\frac{\varepsilon L \cdot D_T}{U_{sup}} \left(\frac{\lambda_n}{R}\right)^2\right]$$

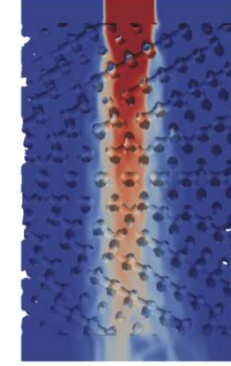


$U_{sup} = 0.3 \text{ m/s}$



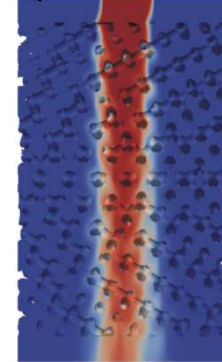
$D_T = 2.27 \times 10^{-4} \text{ m}^2/\text{s}$

$U_{sup} = 0.03 \text{ m/s}$



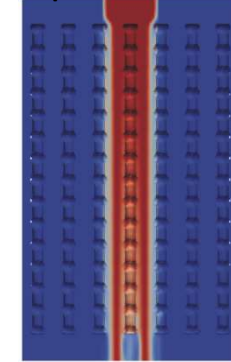
$D_T = 1.52 \times 10^{-5} \text{ m}^2/\text{s}$

$U_{sup} = 0.003 \text{ m/s}$



$D_T = 1.10 \times 10^{-6} \text{ m}^2/\text{s}$

$U_{sup} = 0.03 \text{ m/s}$



$D_T = 6.06 \times 10^{-6} \text{ m}^2/\text{s}$

## CFD simulations – surface reaction

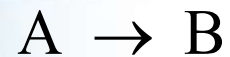
$$U_{\text{sup}} = 0.03 \text{ m/s}; k_r = 0.1 \text{ s}^{-1}$$

### Species

A – reagent

B – product

### Reaction



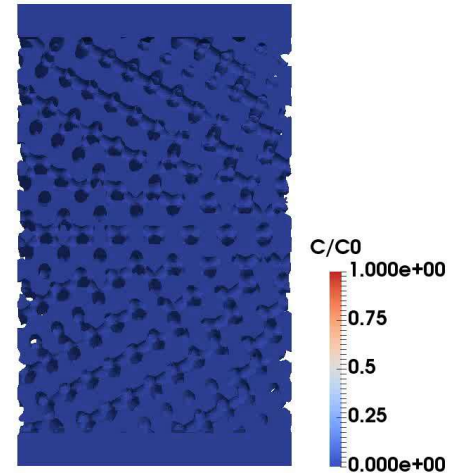
$$r_A = -k_r \cdot C_A$$

### Fluid

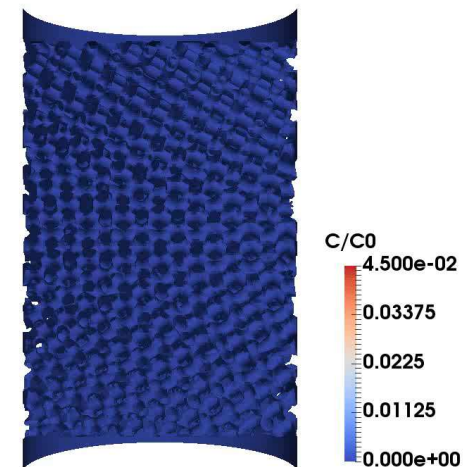
Water properties

$$D_m = 1 \times 10^{-9} \text{ m}^2/\text{s}$$

**A**



**B**





## CFD simulations – fluid phase reaction

### Species

A – reagent  
 B – reagent  
 C – product  
 D – inert

### Reaction



$$r_A = -k_r \cdot C_A \cdot C_B$$

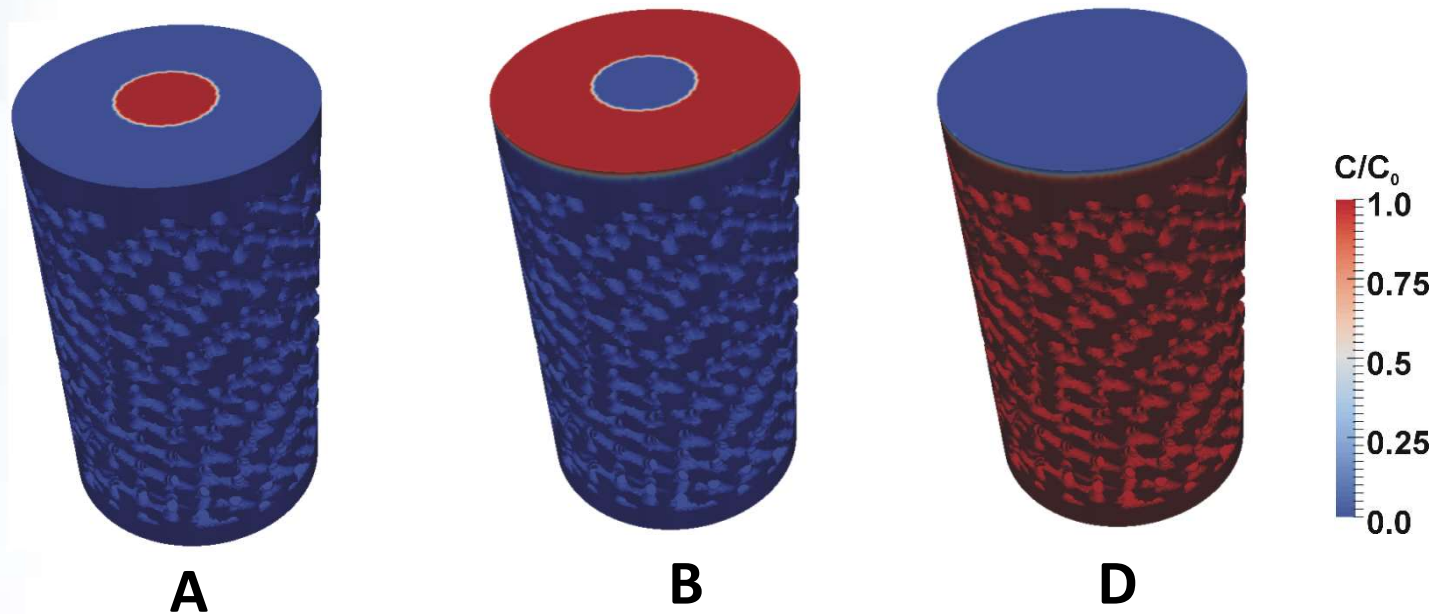
$$-\Delta H_r = 500 \text{ kJ/mol}$$

### Fluid

Water properties

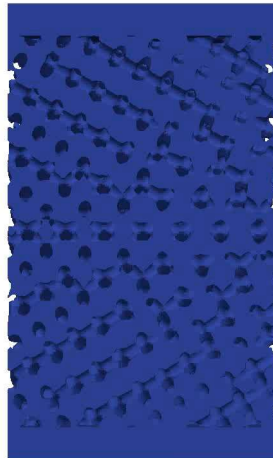
$$D_m = 1 \times 10^{-9} \text{ m}^2/\text{s}$$

$$T_{in} = 373 \text{ K}$$

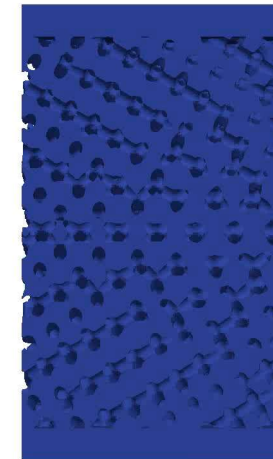


## CFD simulations – fluid phase reaction

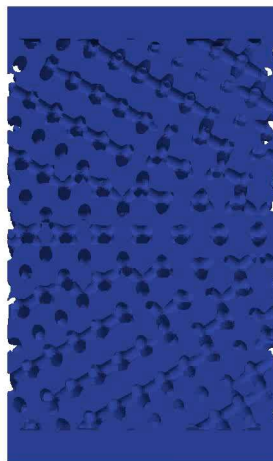
A



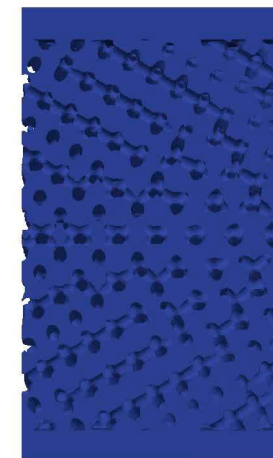
B



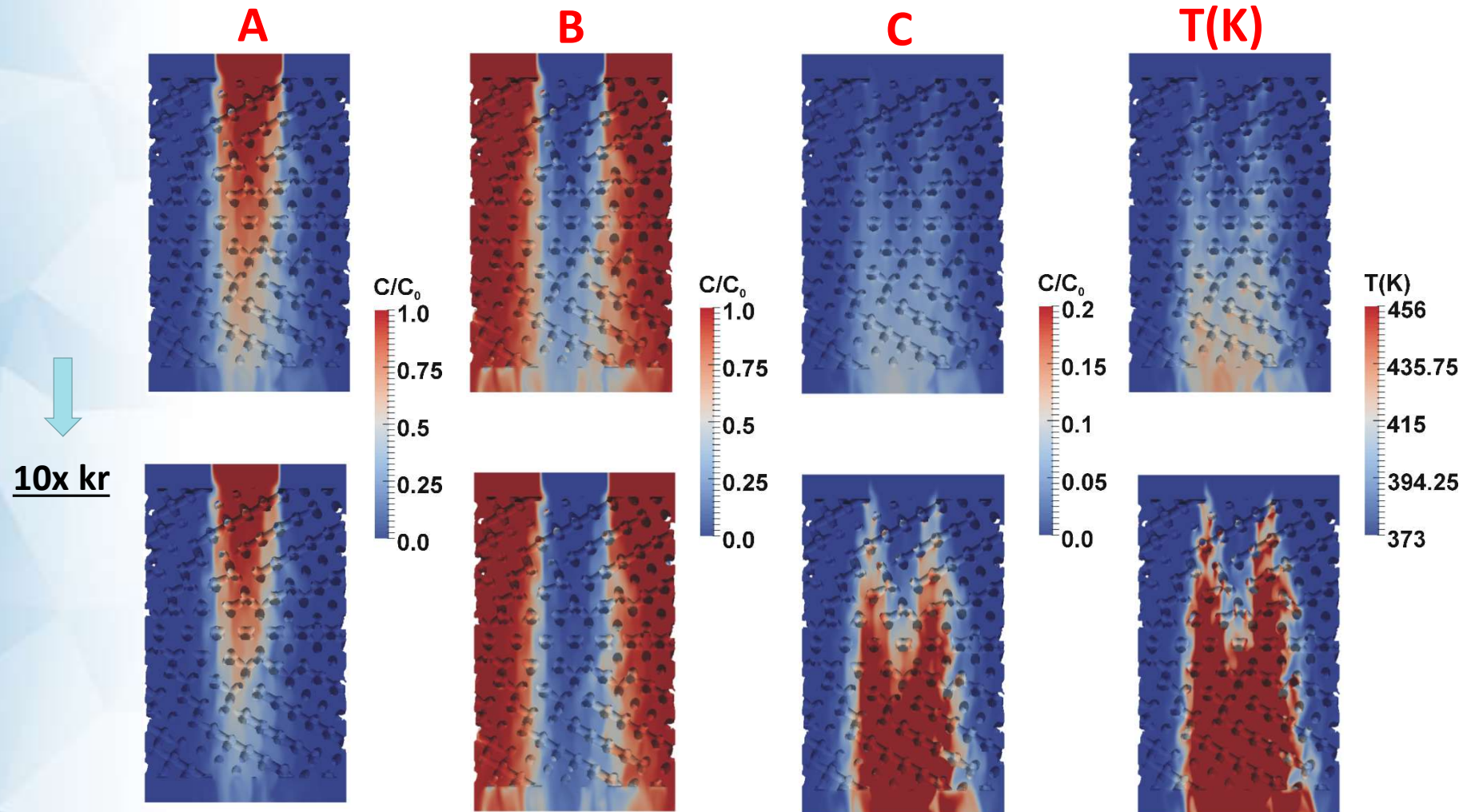
C



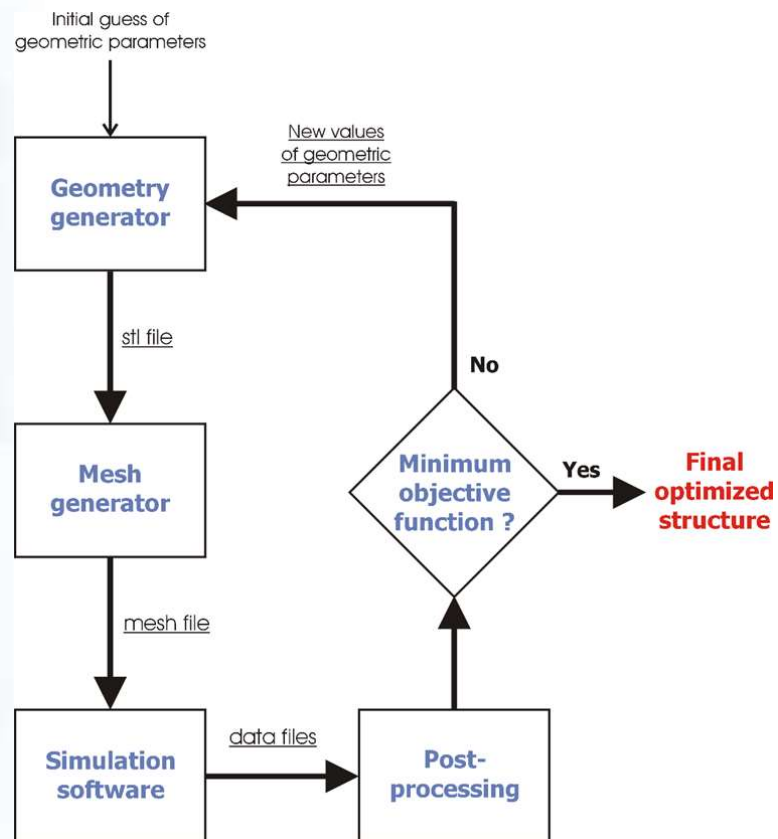
T(K)



## CFD simulations – fluid phase reaction



## Optimization procedure



**Fully automatic**

Input – initial parameter values

Output – stl file with optimized shape

**Couples several tools**

Geometry generator

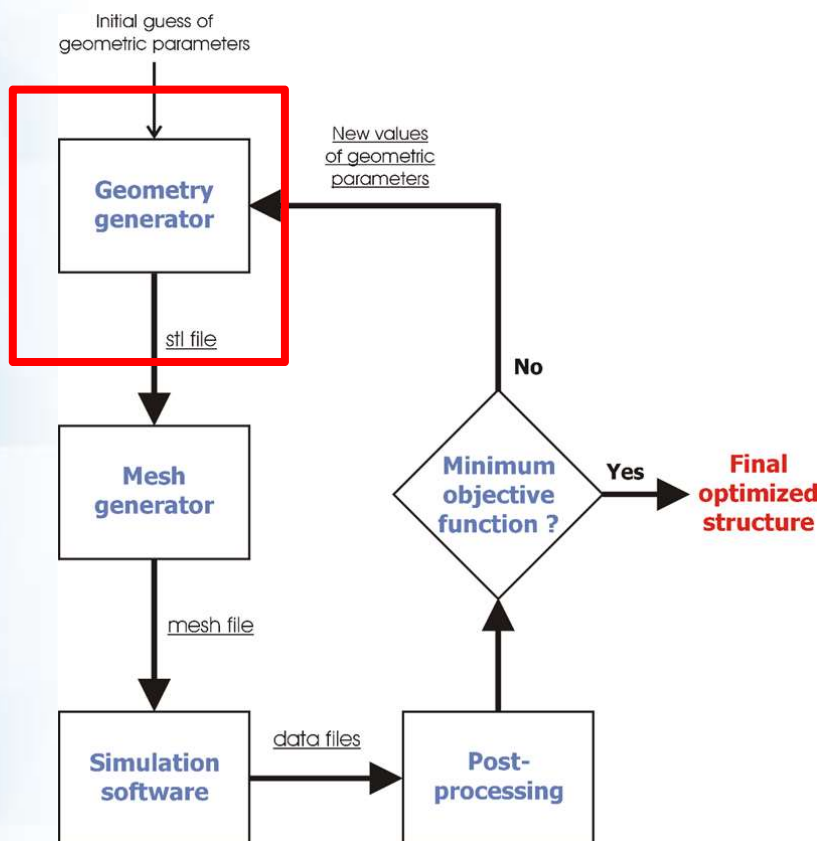
CFD software

Optimizer

**Versatile**

Useful for optimization of different types of systems and process units

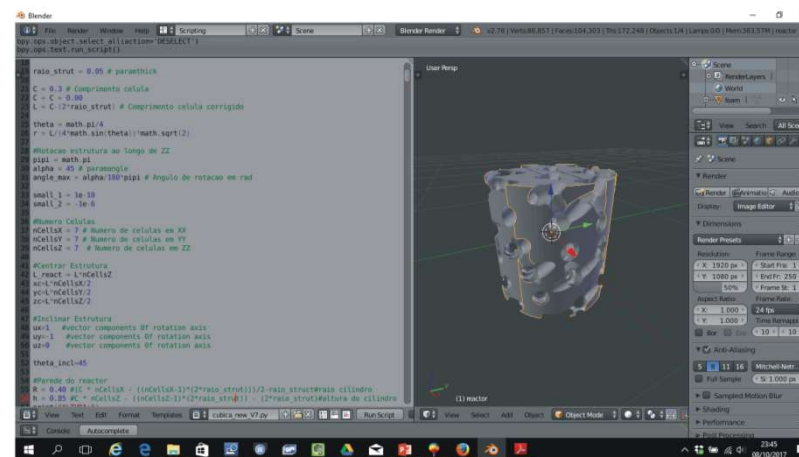
## Optimization procedure



## 1 - Shape generation

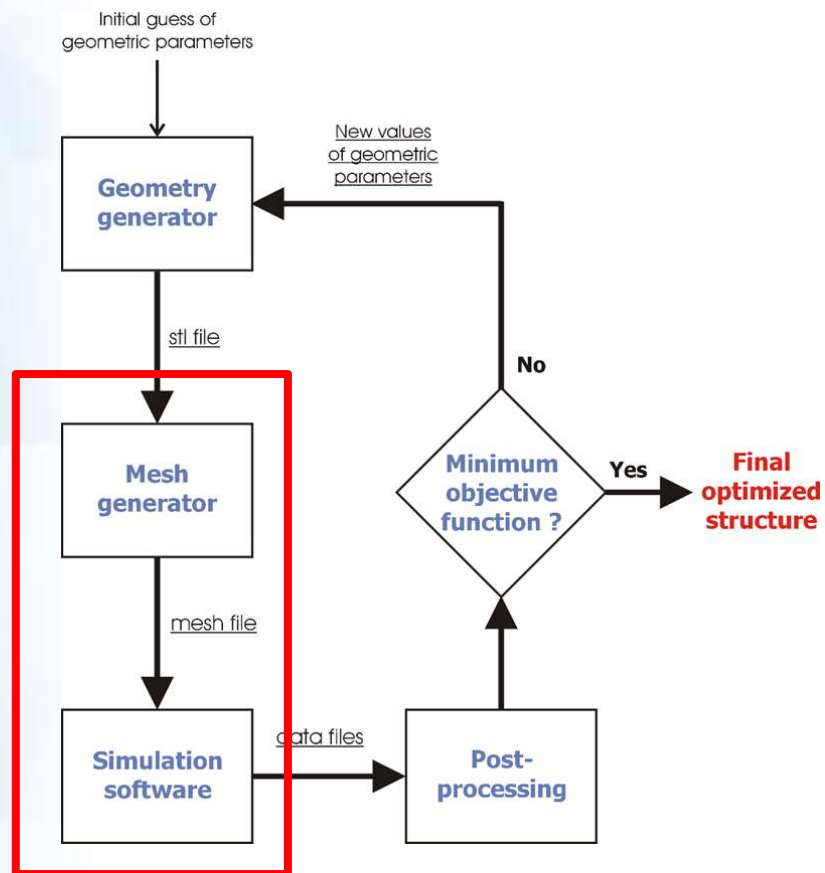
Blender® software (freeware)

Python script (each one for a different topology)



**Stl files**

## Optimization procedure



## 2 – CFD tools

OpenFOAM® software (freeware)

Communication with other blocks – application of bash scripts

Language – C++

Meshing – cfMesh or snappyHexMesh tools

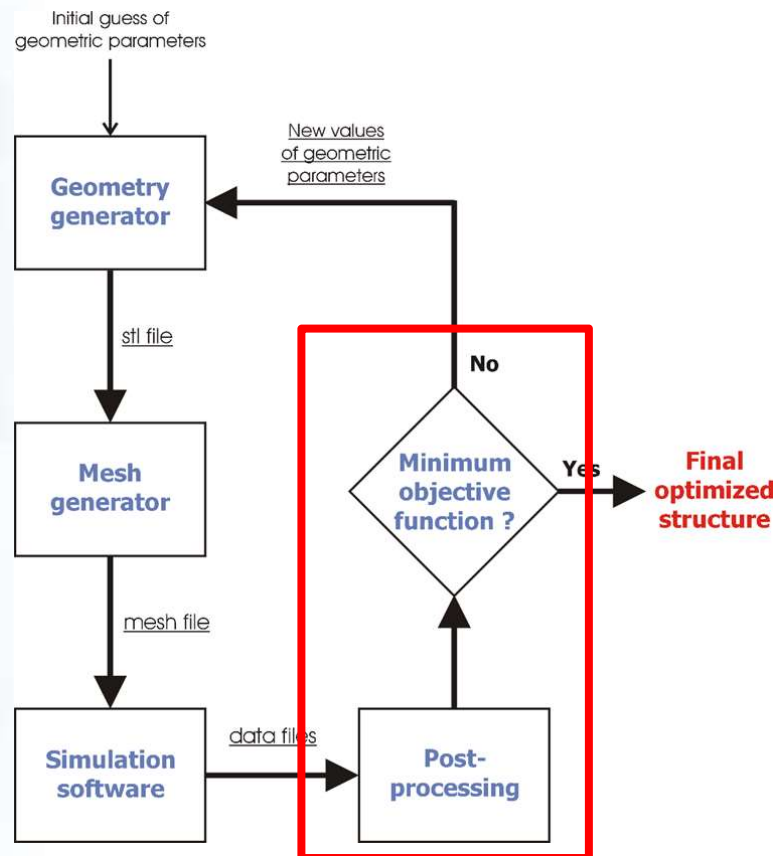
Solver – Single-phase flow with heat and mass transfer

Cyclic BC – to benefit from the periodicity of flow field in open channel structures



data files

## Optimization procedure



## 3 – Post-processing

Evaluation of an objective function that synthesizes the limitations and/or goals of the process

$$\star F_{obj} = w_C \cdot \frac{\sum |C_{out} - \bar{C}_{out}|}{\sum C_{out}} + w_T \cdot \frac{\sum |T_{out} - \bar{T}_{out}|}{\sum T_{out}} + w_P \cdot (P_{in} - P_{out}) + w_A \cdot \frac{V_{total}}{A_S}$$

Nomad® optimizer (freeware)

new parameter values

# Acknowledgements

## PRINT CREDIT

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